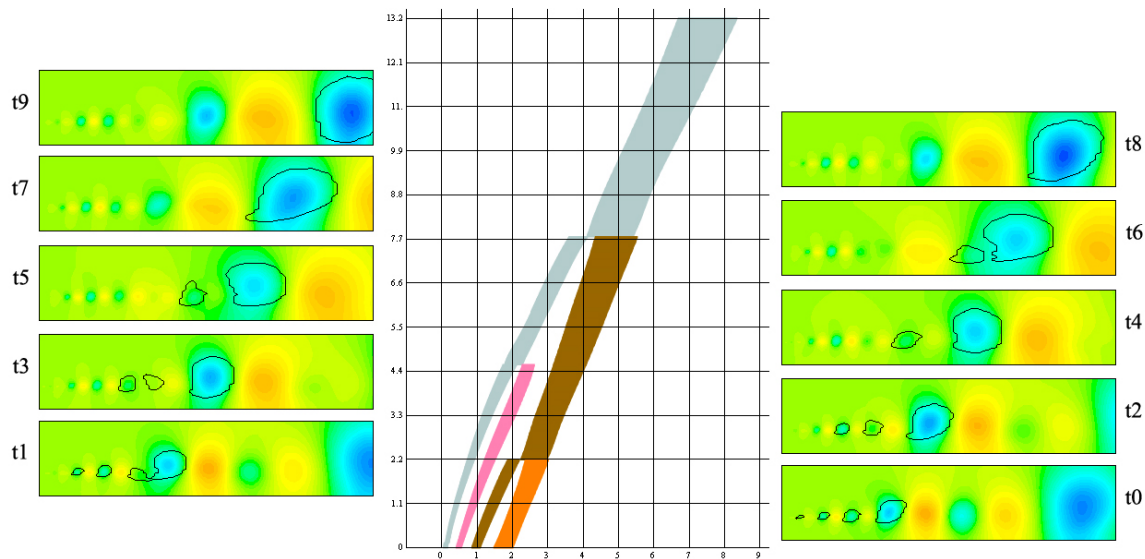


Quantifying Coherent Structures in Large-Eddy Simulation

Máté Márton LOHÁSZ

László NAGY, Péter TÓTH, István KONDOR

Dept. of Fluid Mechanics @ Budapest University of Technology and Economics



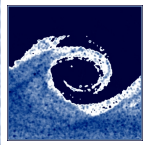
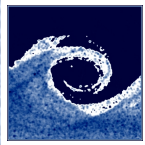


Table of contents

- The coherent structure concept
- Q as vortex detection criteria
- Investigation methods
 - Image processing
 - Ribbed duct
 - Conditional averaging
 - Channel flow
 - Ribbed duct
 - Vortex tracking
 - Axisymmetric jet
 - Spinning, merging vortex pair



Coherent structure concept

Coherent structure (CS) concept:

Turbulent motion can be decomposed into three parts

Reynolds decomposition

$$\varphi = \bar{\varphi} + \tilde{\varphi}$$

Triple decomposition

$$\varphi = \bar{\varphi} + \tilde{\varphi}_c + \tilde{\varphi}_b$$

$\bar{\varphi}$

Average

$$\tilde{\varphi} = \tilde{\varphi}_c + \tilde{\varphi}_b$$

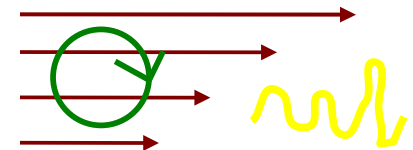
Fluctuation

$\tilde{\varphi}_c$

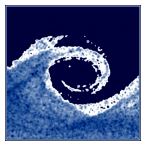
Coherent motion

$\tilde{\varphi}_b$

Turbulent background



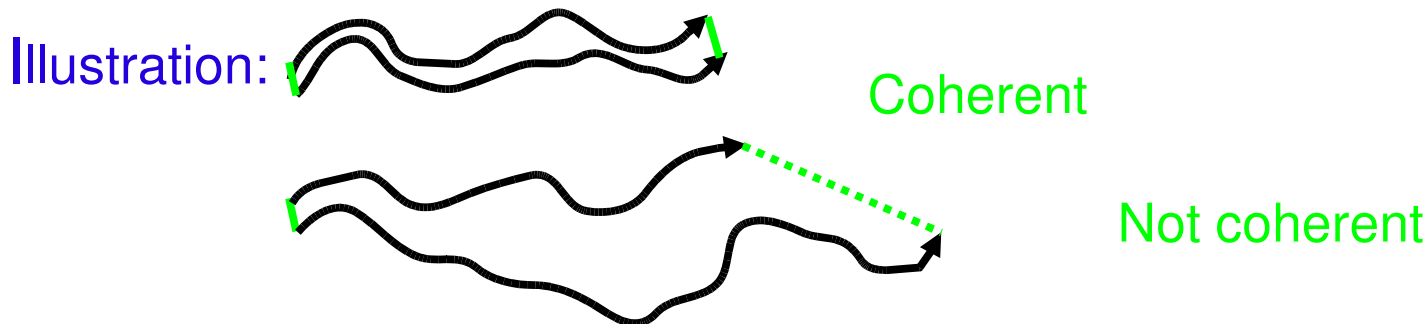
An important part of the fluctuation can be characterised by the motion of regular fluid structure so called **coherent structures**



Vortices are coherent structures

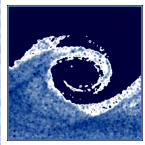
- The vortices are the coherent (does not change much in space and time) structure in fluid motion

Chakraborty2005, Haller2005 gives the mathematical proof



- How to find vortices in 3D flowfields?

To select quantities which are related to rotating motion



Q vortex detection criteria

Q criteria: (Hunt1988)

➤ Regions of $Q > Q_{th} > 0$ with local

pressure minima **is defined as vortex**

➤ Only a fraction of the rotating fluids is defined as a vortex

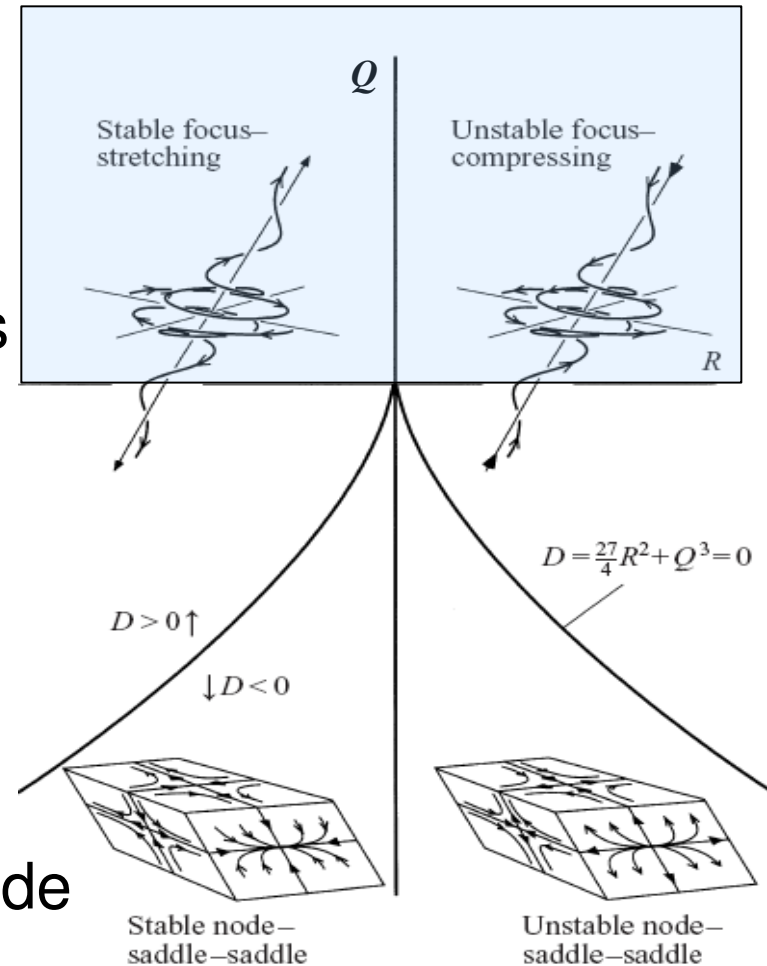
$$Q = -\frac{1}{2} A_{ij} A_{ji} = \frac{1}{2} (\Omega_{ij} \Omega_{ji} - S_{ij} S_{ji})$$

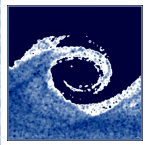


Vorticity dominance

$Q > 0$ means vorticity dominance

➤ Charkaborty2005 showed that beside $D > 0$, $Q > 0$ is needed for coherence





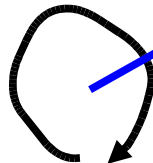
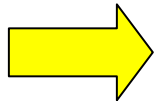
Q vortex detection criteria

Q is the source term in the Poisson equation for pressure

Pressure equation:

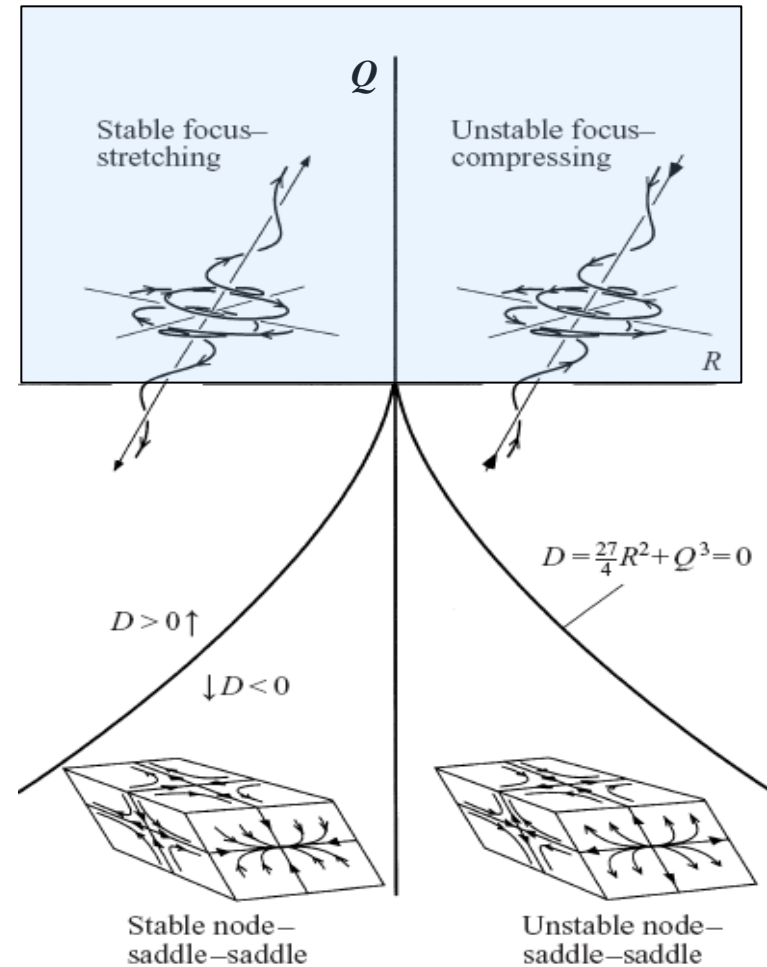
$$\Delta p = 2\rho Q$$

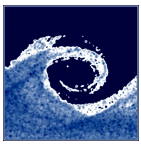
Source term



$$\frac{\partial p}{\partial n} < 0$$

Pressure is lower in the centre of the vortex

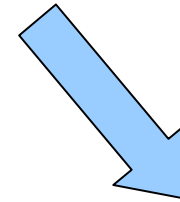




What to do with the coherent structures?

Traditional technology: Image processing

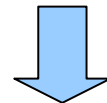
- 1) Create movies of the temporal evolution of the vortices with different thresholds, and different viewpoints
- 2) Find “well known” features
- 3) Quantify what you can
- 4) Compare to possibly existing theory



Drawback:

“only” qualitative results

- 1) Result is user dependent
- 2) Evolution described in a poetic way e.g. :
”One sees vortices passing by as a flight of big migratory birds” (Lesieur2003)



Methods are needed to quantify coherent structure evolution

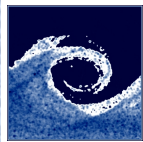
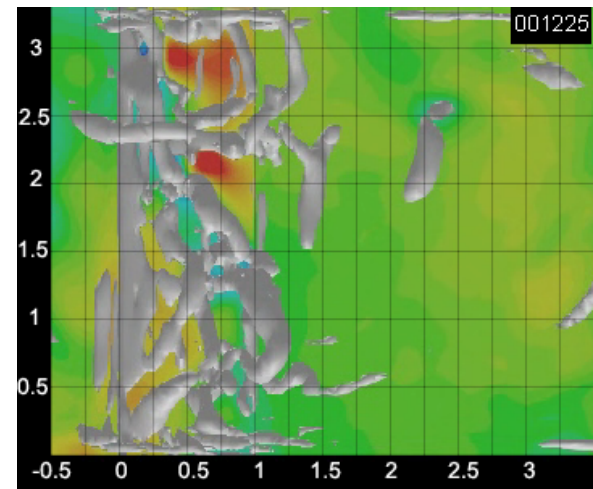
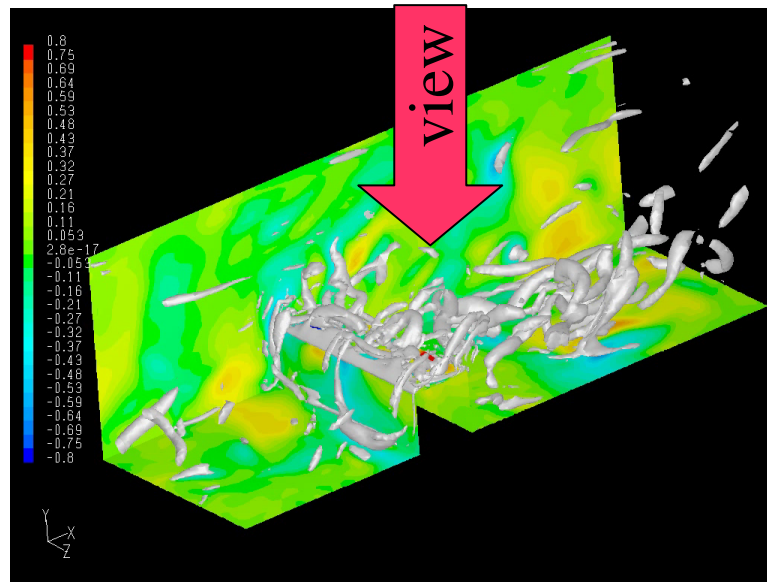
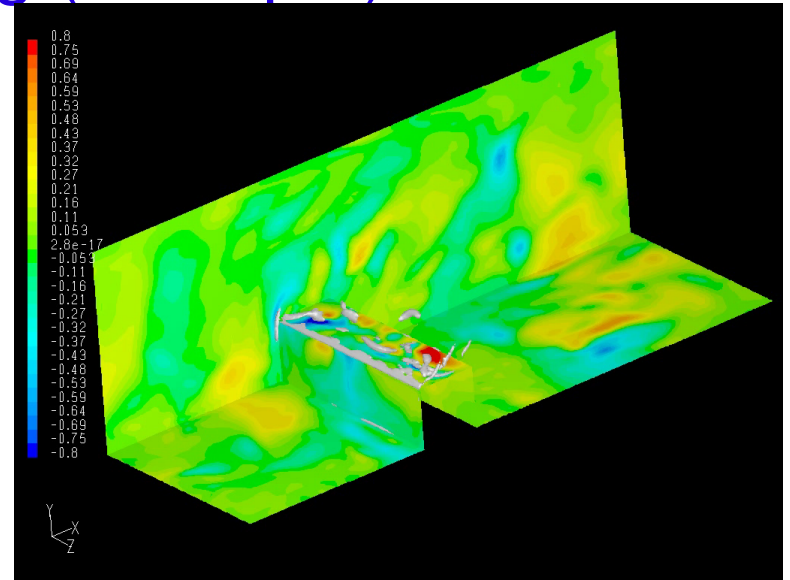
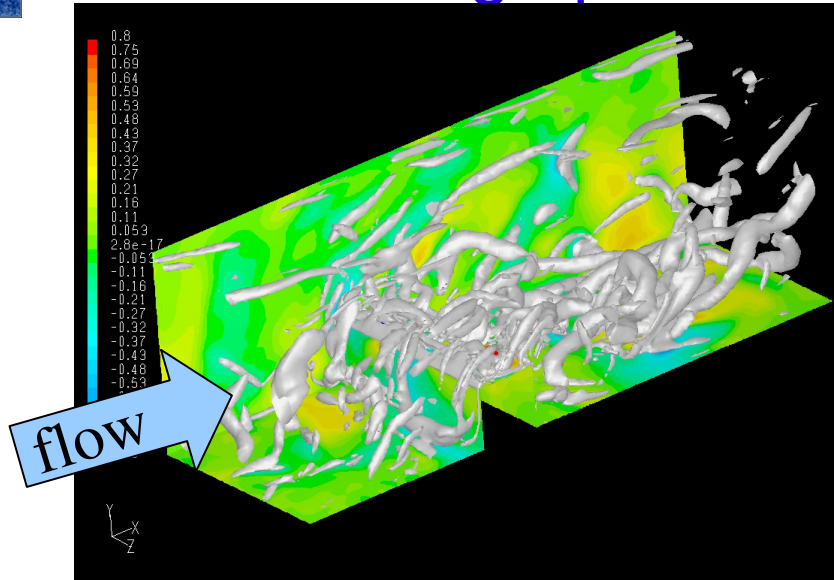
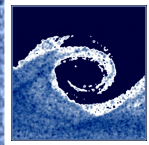


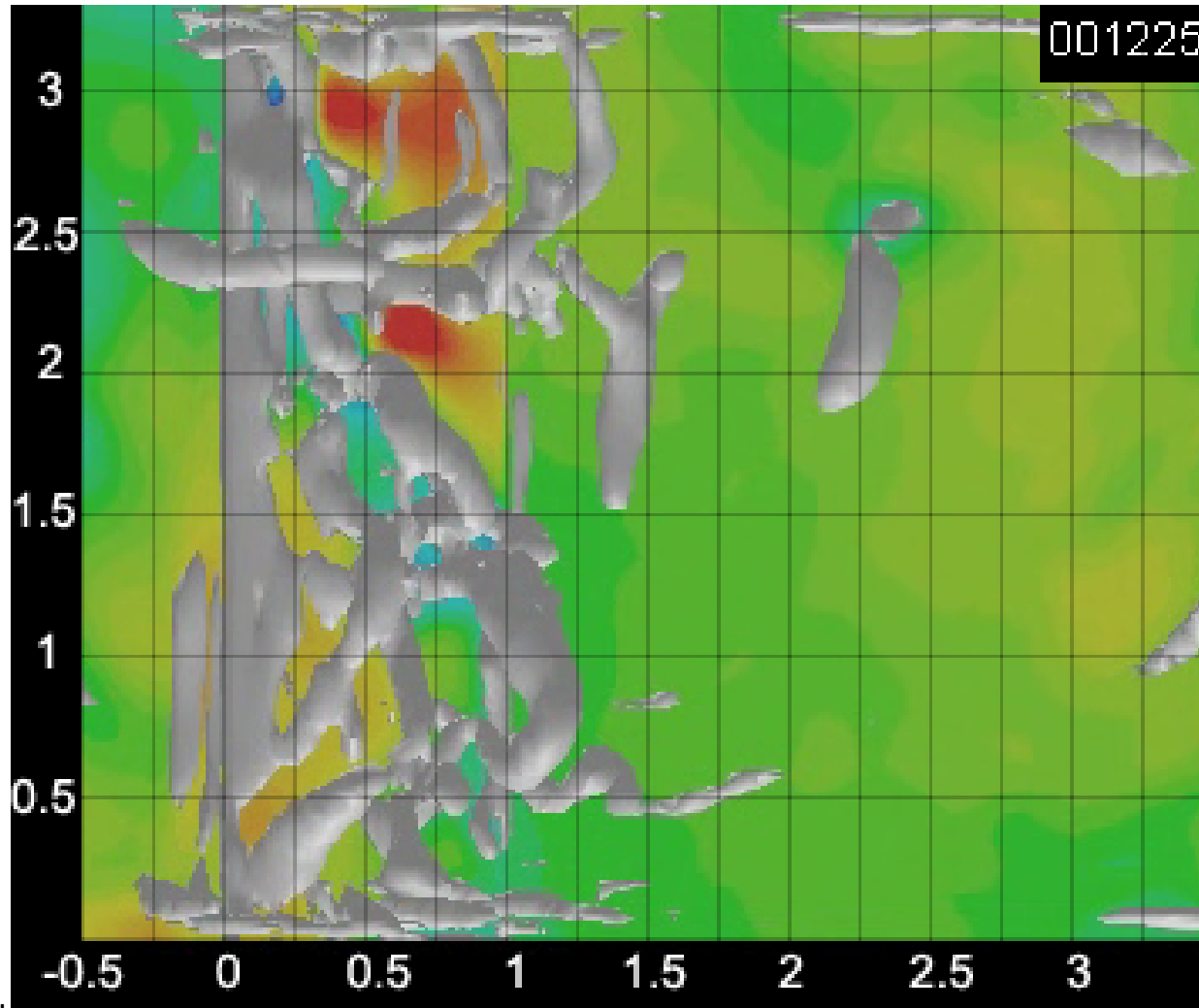
Image processing (example)

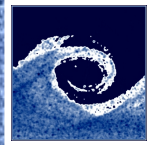




Distance between the structures above the rib

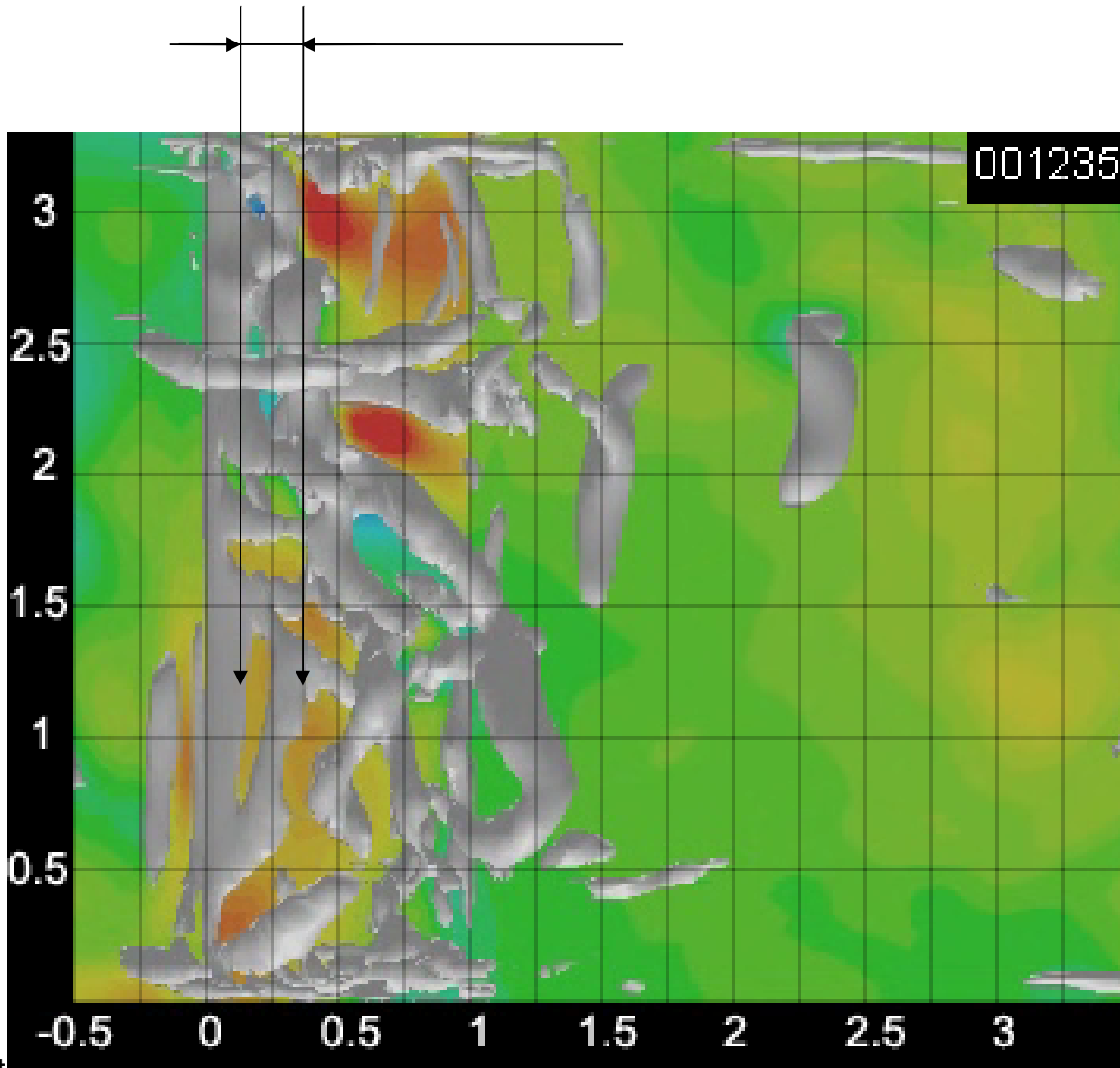
Changes between 0.2-0.3h

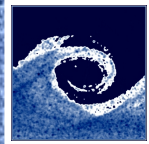




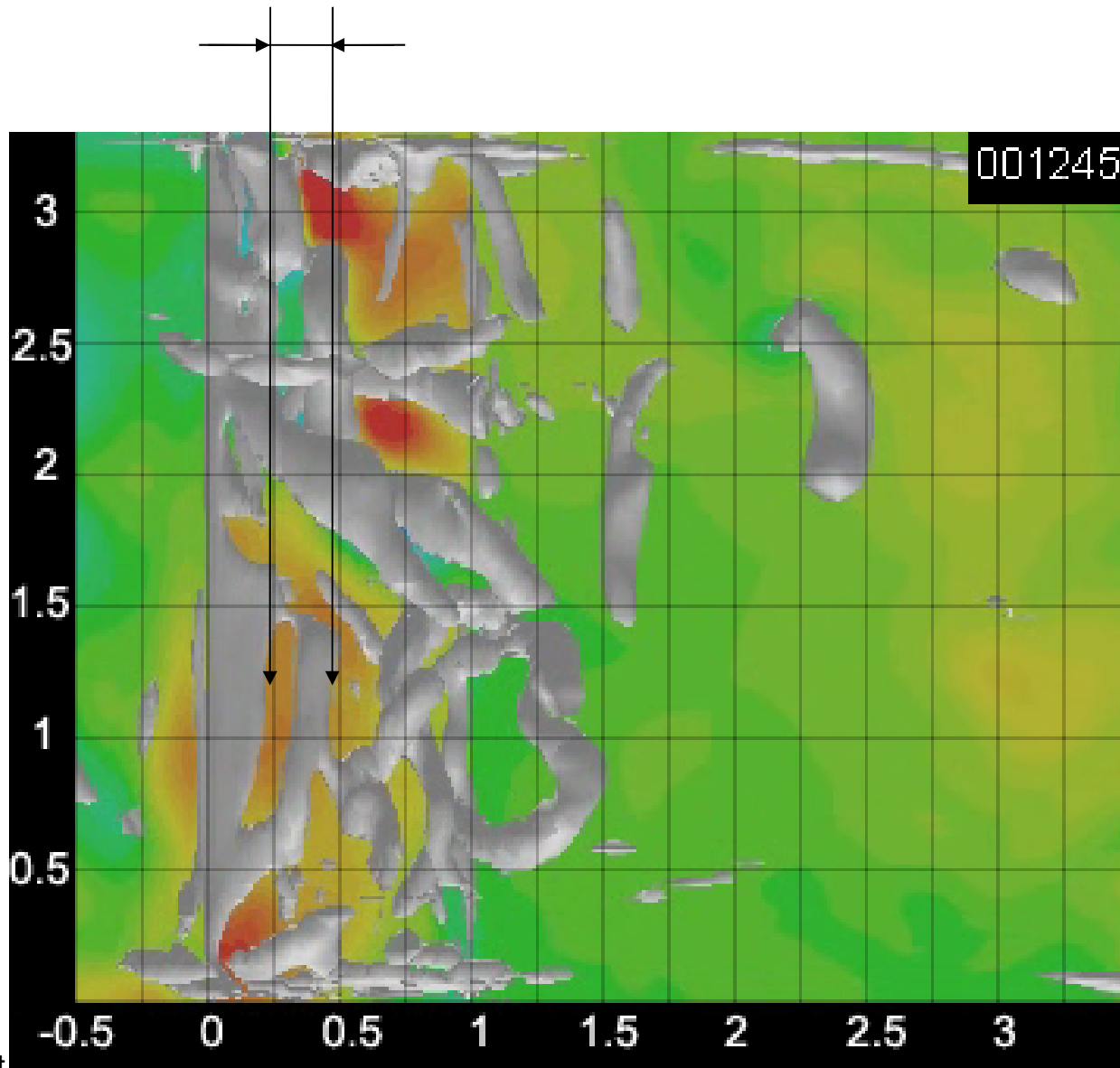
Distance between the structures above the rib

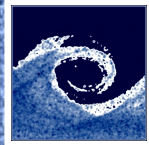
$0.3 h$



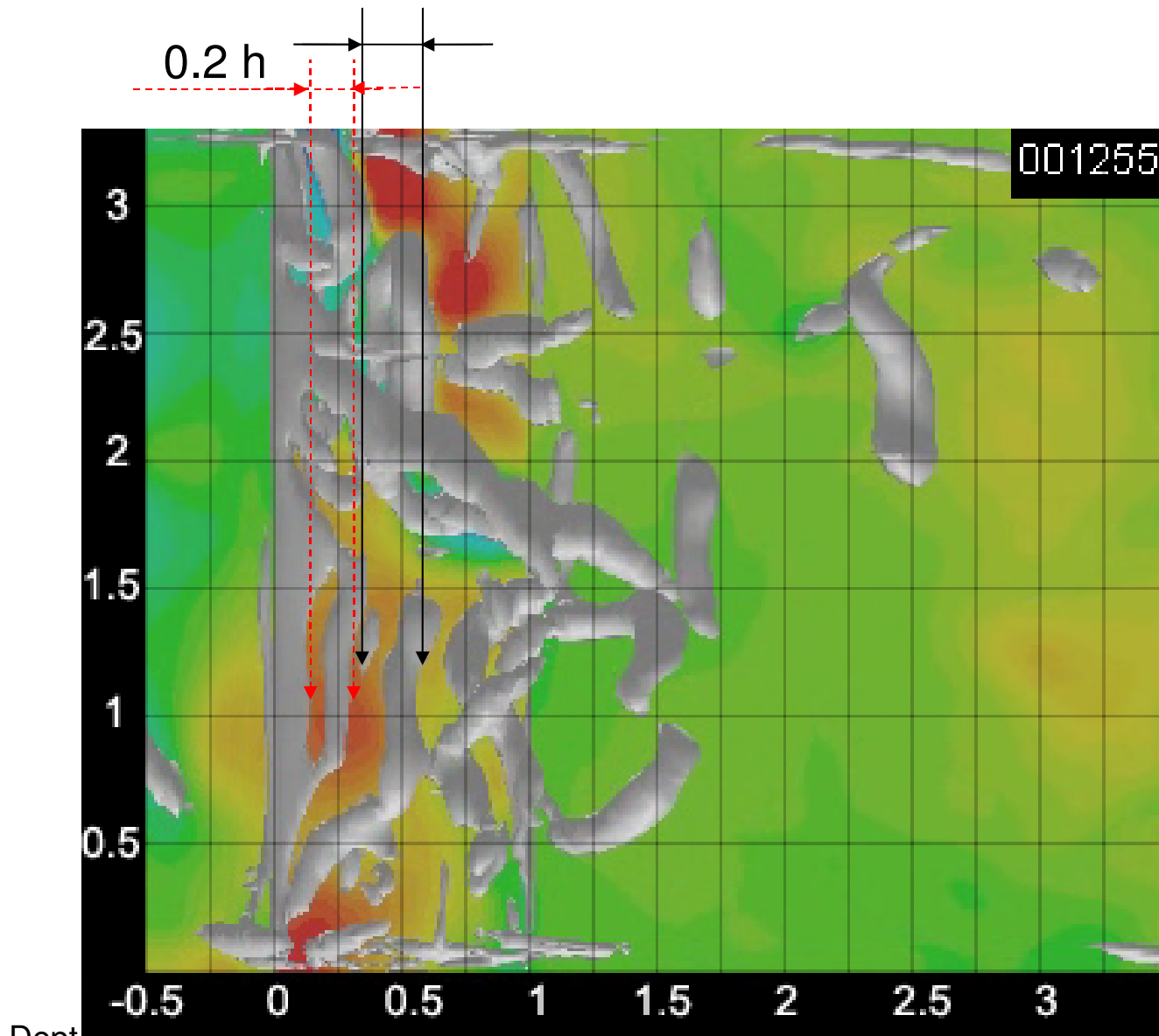


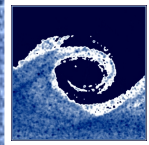
Distance between the structures above the rib



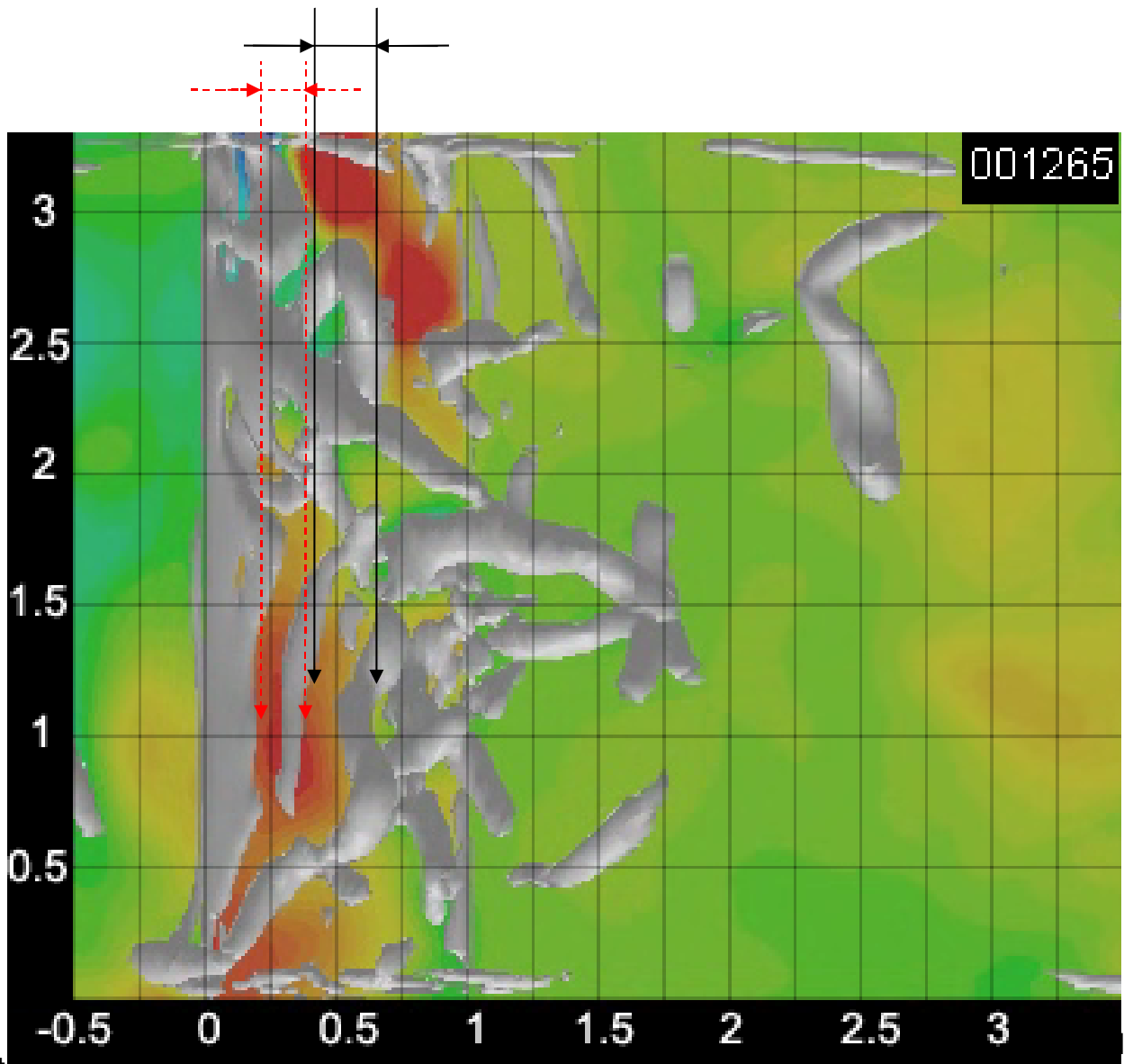


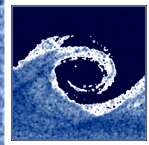
Distance between the structures above the rib



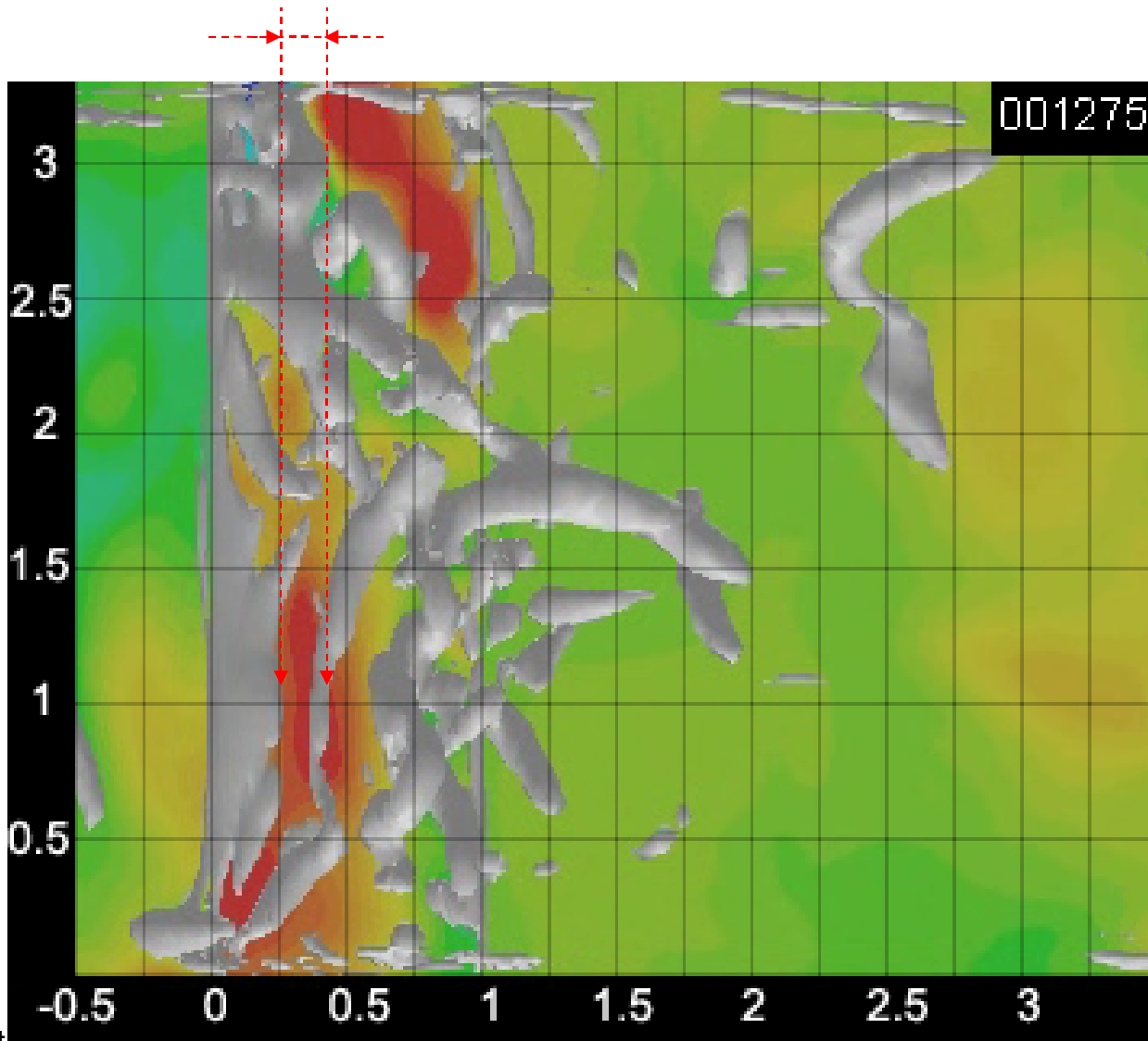


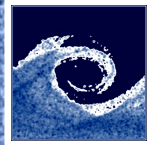
Distance between the structures above the rib



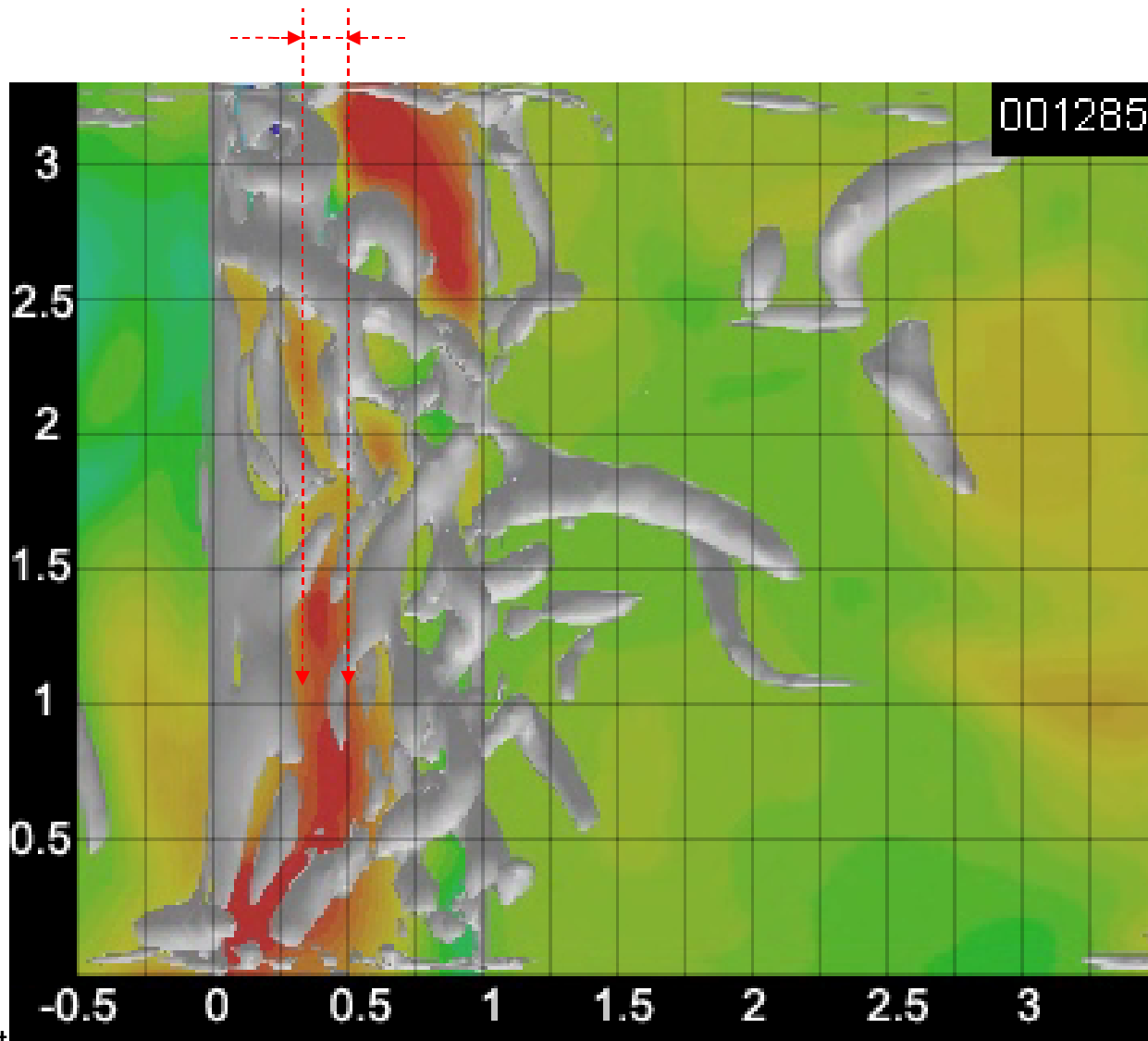


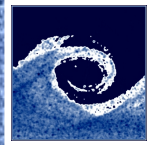
Distance between the structures above the rib





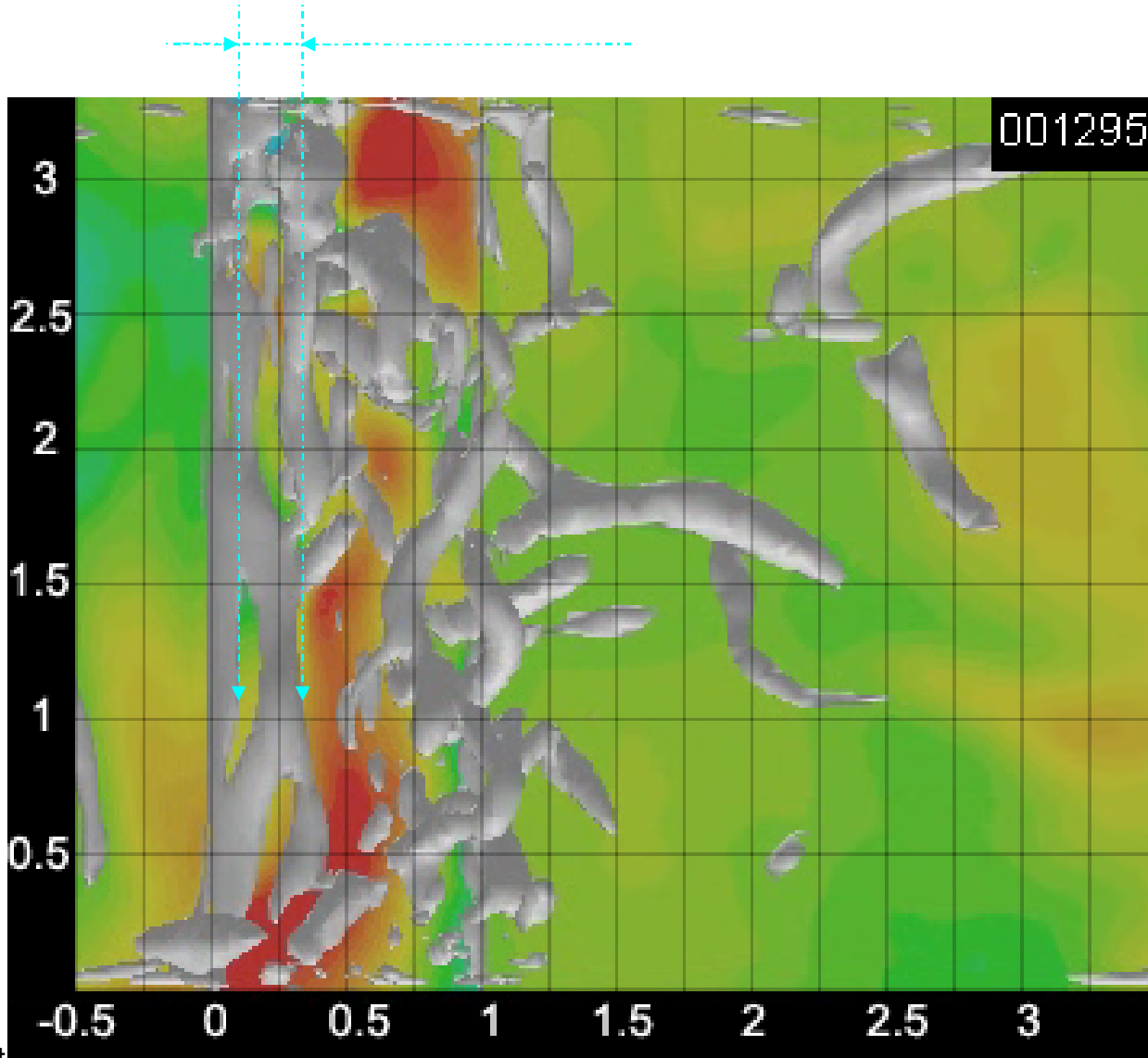
Distance between the structures above the rib

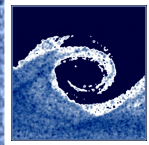




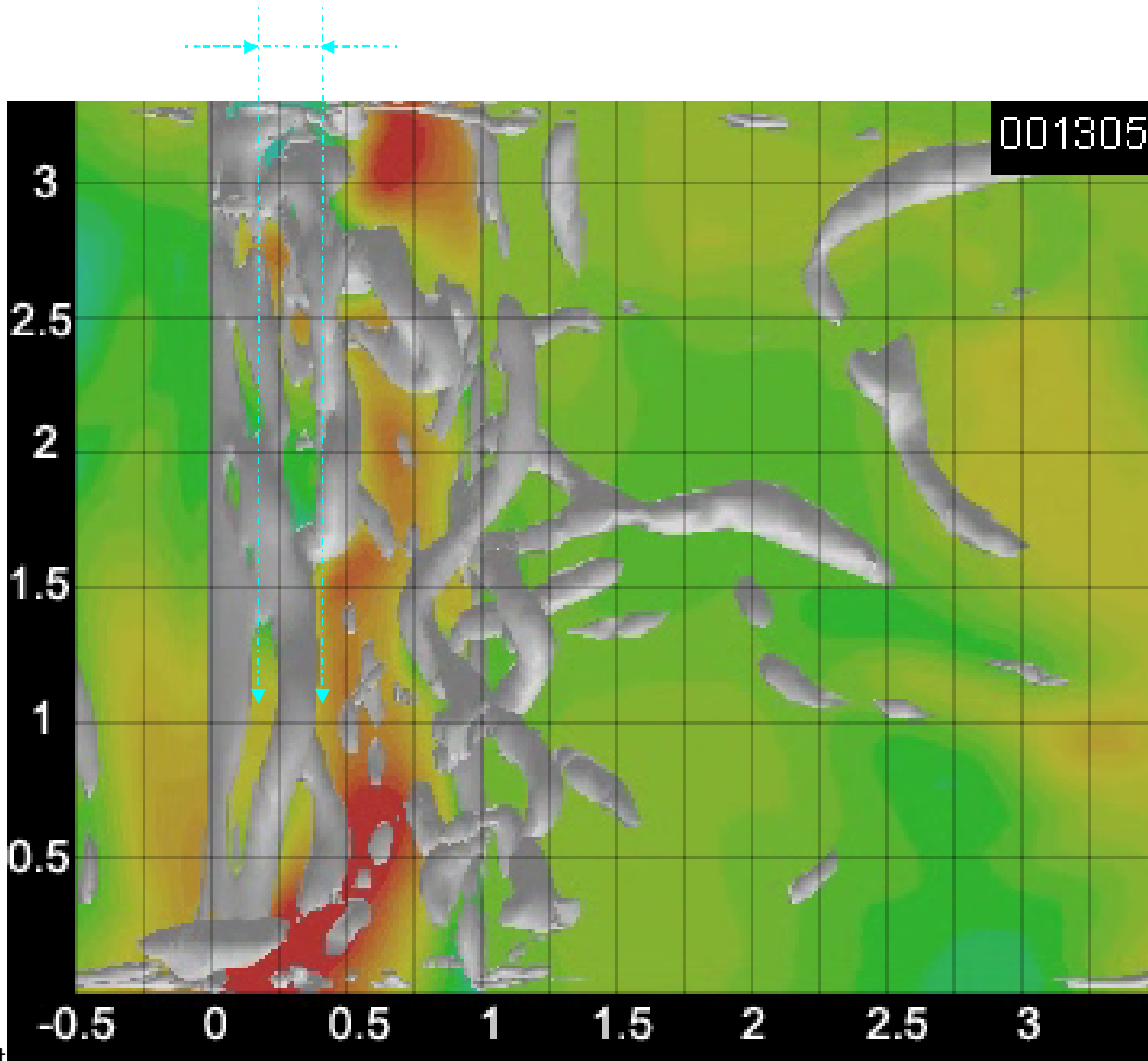
Distance between the structures above the rib

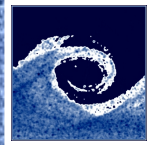
0.3 h



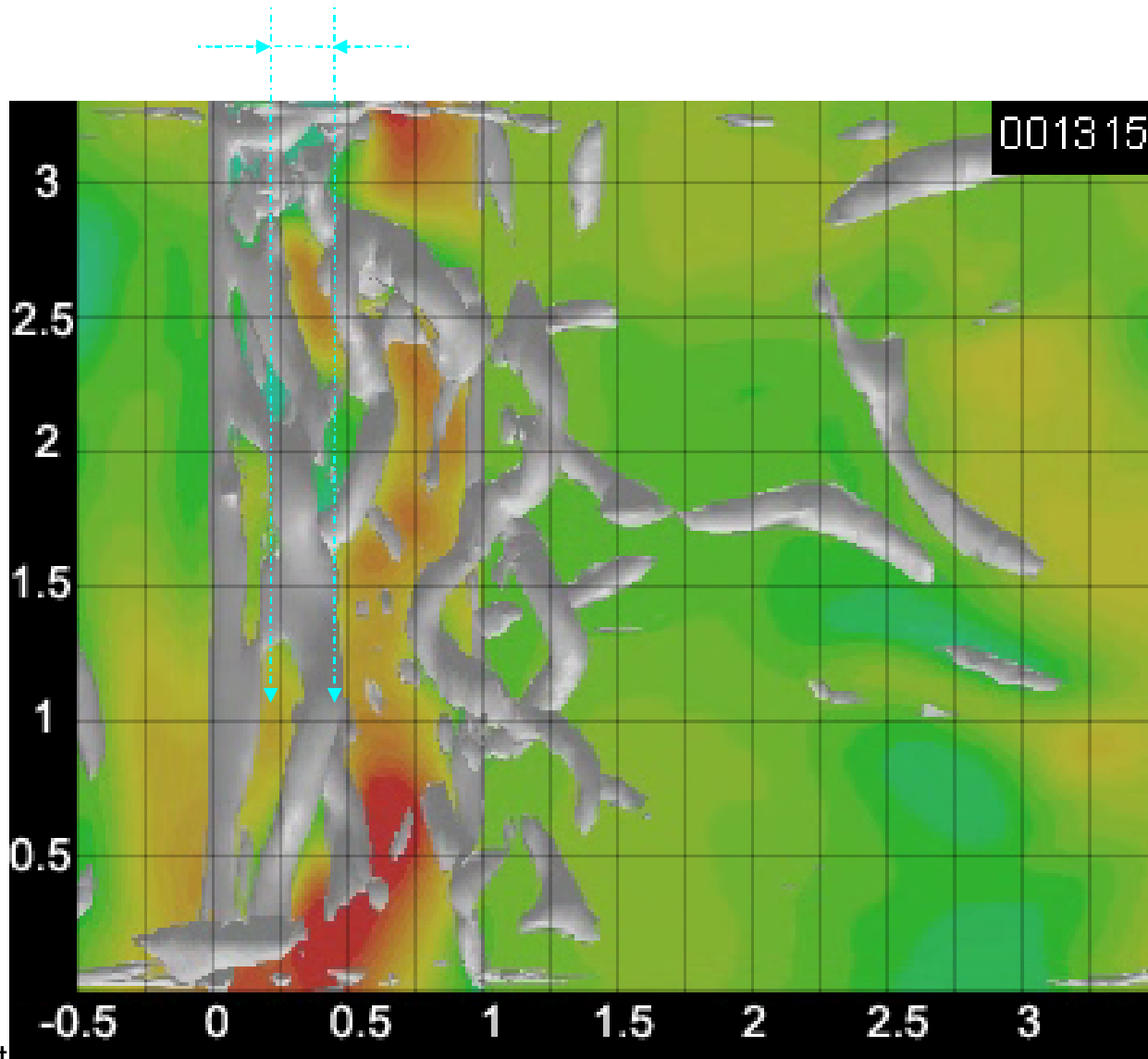


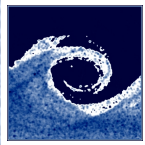
Distance between the structures above the rib





Distance between the structures above the rib





Conditional averaging

Indicator function:

$$I_\alpha \doteq \begin{cases} 1 & Q(\mathbf{x}, t) \in Q_\alpha \\ 0 & Q(\mathbf{x}, t) \notin Q_\alpha \end{cases}$$

The classes:

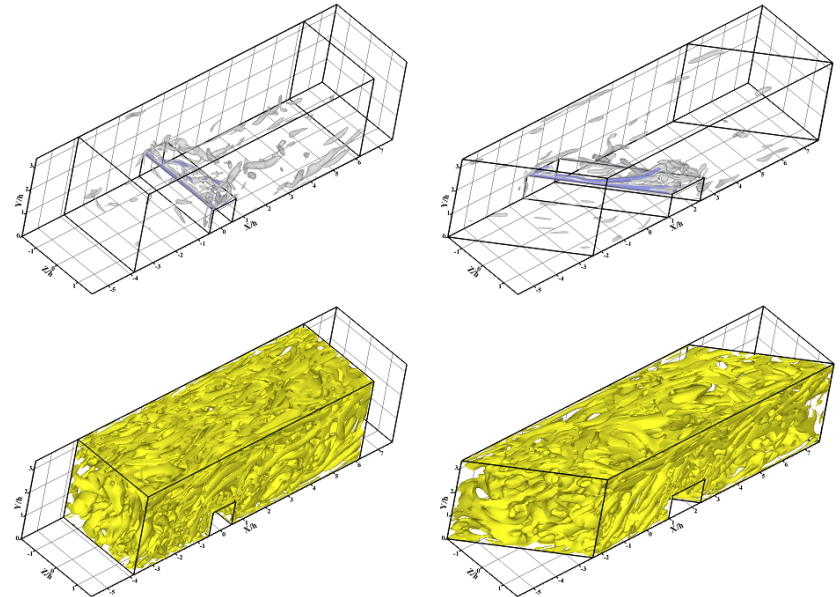
- $Q_I \doteq \{x : x \in \mathbb{R} \wedge x < 0\}$
- $Q_{II} \doteq \{x : x \in \mathbb{R} \wedge 0 < x < 200\}$
- $Q_{III} \doteq \{x : x \in \mathbb{R} \wedge 200 < x < 1500\}$
- $Q_{IV} \doteq \{x : x \in \mathbb{R} \wedge 1500 < x \}$

Conditional averaged variable:

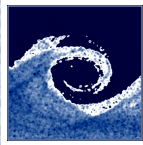
$$\langle \varphi \rangle^\alpha \doteq \frac{\langle \varphi I_\alpha \rangle}{\langle I_\alpha \rangle}$$

Deviation:

$$\Delta^\alpha \varphi = (\langle \varphi \rangle^\alpha - \langle \varphi \rangle)$$



(Lohász2005)

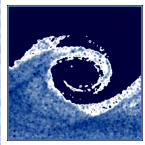


Probability of the classes

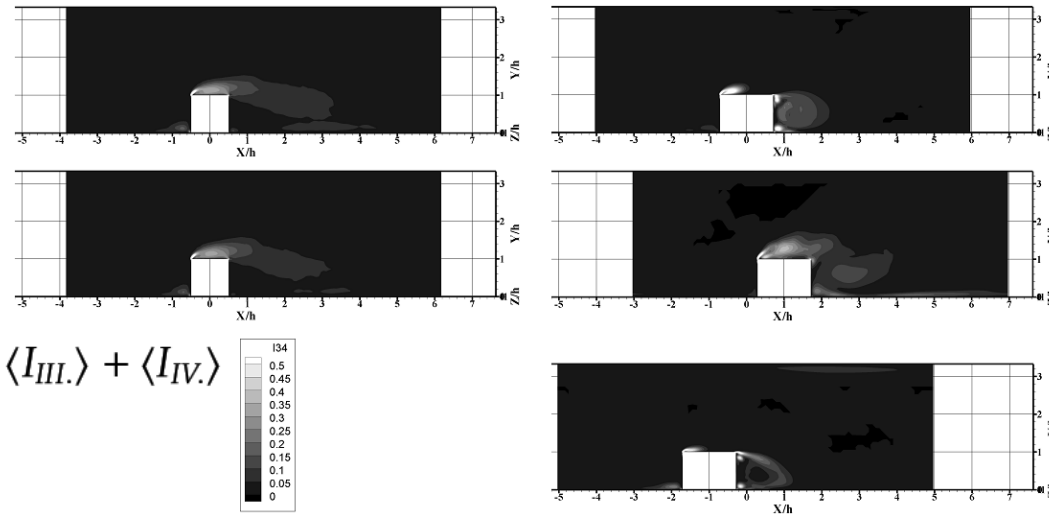
Class	Definition	90° Case	45° Case
I.	$Q < 0$	0.6	0.597
II.	$0 < Q < 200U_b^2/D_h^2$	0.376	0.388
III.	$200U_b^2/D_h^2 < Q < 1500U_b^2/D_h^2$	0.019	0.014
IV.	$Q > 1500U_b^2/D_h^2$	0.0008	0.0009
III.+IV.	$Q > 200U_b^2/D_h^2$	0.02	0.015

More background than vortex for both cases

Intense vortices are more probable for perpendicular rib



Location of the intense vortices



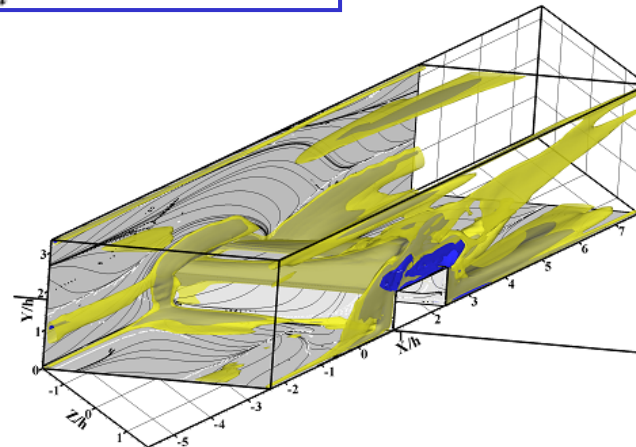
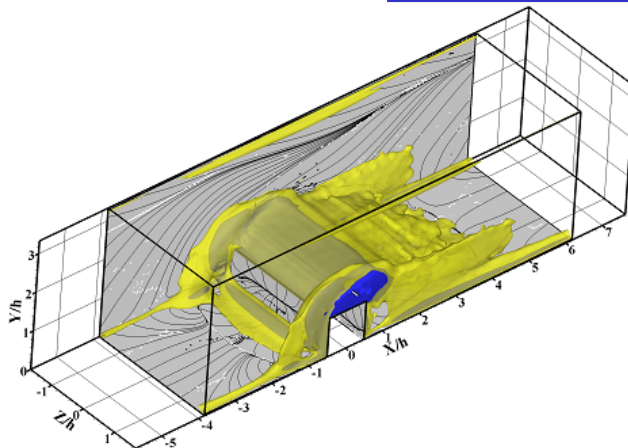
$Z/h = 0$

$Z/h = 1$

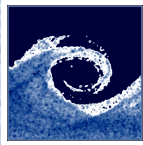
$Z/h = -1$

- Leading edge of the rib
- Shear layer of 90° rib
- Wake of the 45° rib

$$Q > 200U_b^2/D_h^2 \text{ class } (\langle I_{III.} \rangle + \langle I_{IV.} \rangle)$$



- 10% probability
- 5% probability



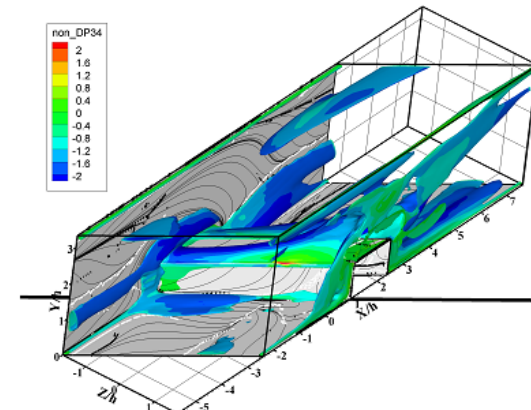
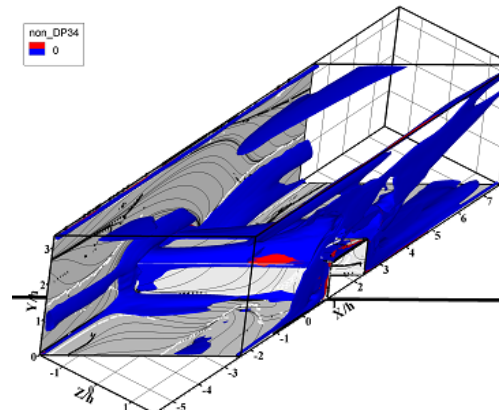
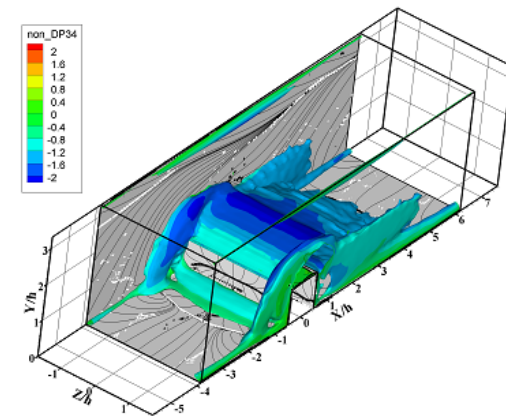
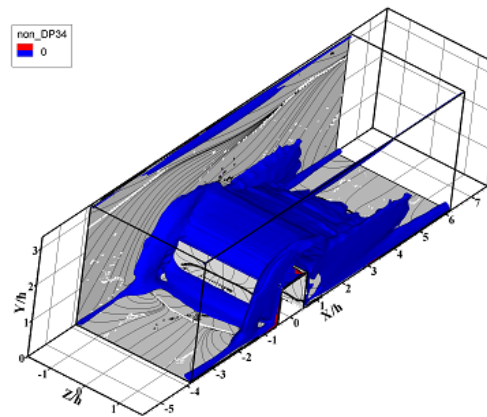
The pressure deviation

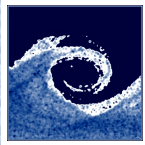
Volume average of the pressure deviation for each class for the higher than 5% probability regions

Class	$\Delta^\alpha P$		90°	45°
	90°	45°		
I.	0.208	0.302	1	1
II.	-0.254	-0.391	0.999	0.996
III.	-1.083	-1.435	0.084	0.063
IV.	-1.376	-1.201	0.003	0.003
III.+IV.	-1.134	-1.189	0.085	0.064

Size of the higher than 5% probability regions

Isosurface of $\langle I_{34} \rangle = 0.05$
coloured by $\langle \Delta^{34} P \rangle / \sqrt{\langle p'^2 \rangle}$





Channel flow

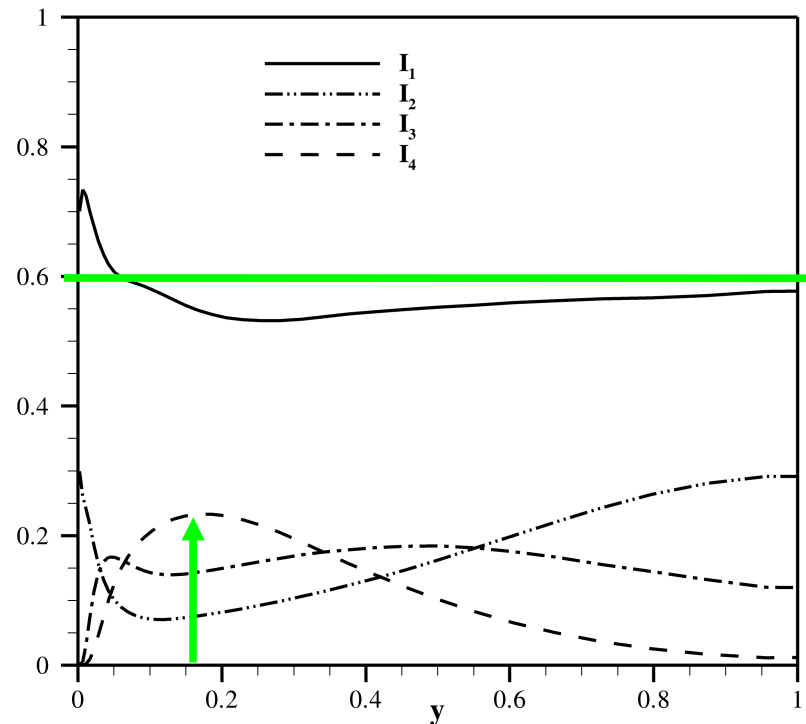
$Re_\tau = 180$

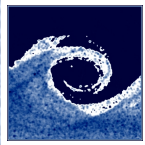
LES with Dyn. Smag.
 72^3 cells
sec. ord. scheme

Q class borders:
 $0, 0.1, 0.01 U_b^2/\delta^2$

- $Q < 0$ is appr. 60%,
i.e vortices are rare
- Intense vortices have
high probability in
buffer zone

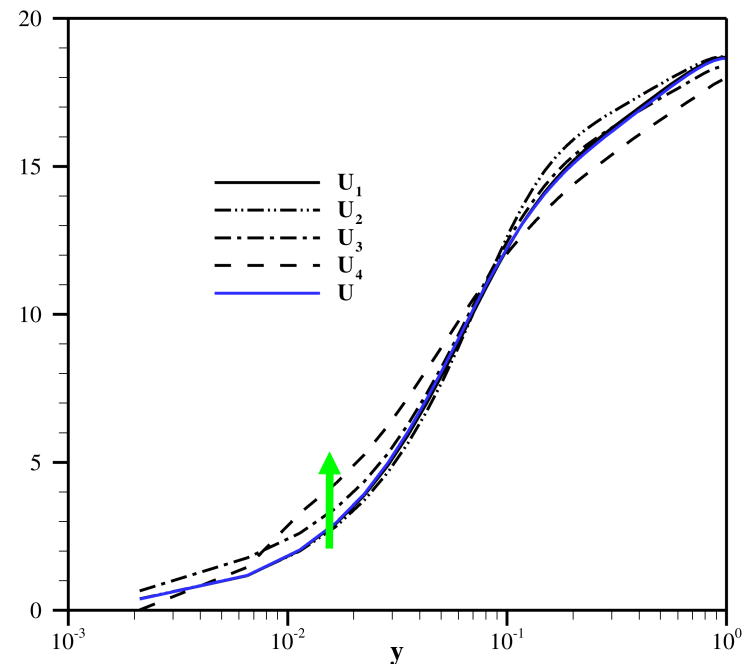
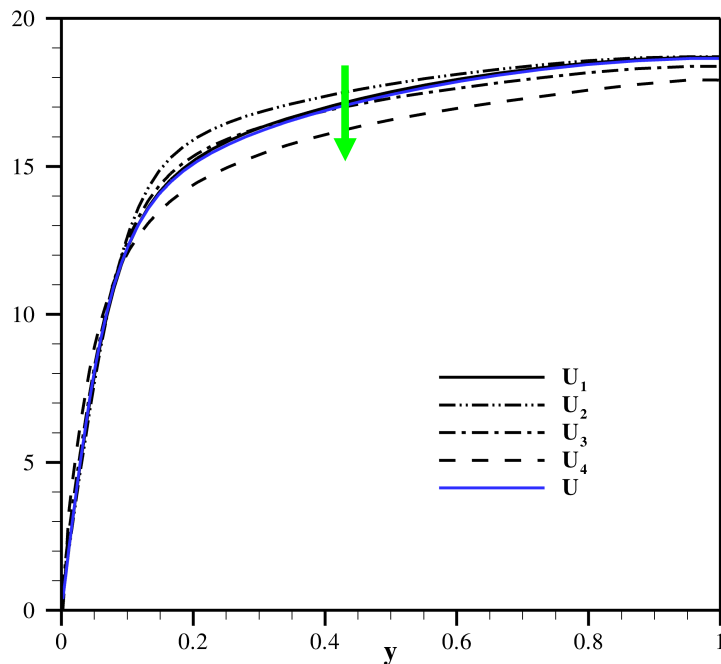
Vortex probability



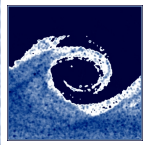


Channel flow

Streamwise velocity



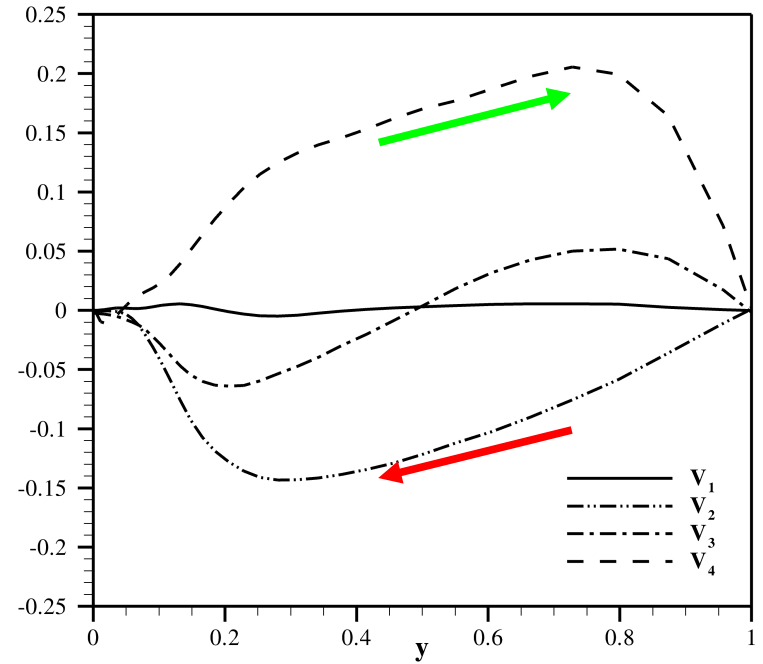
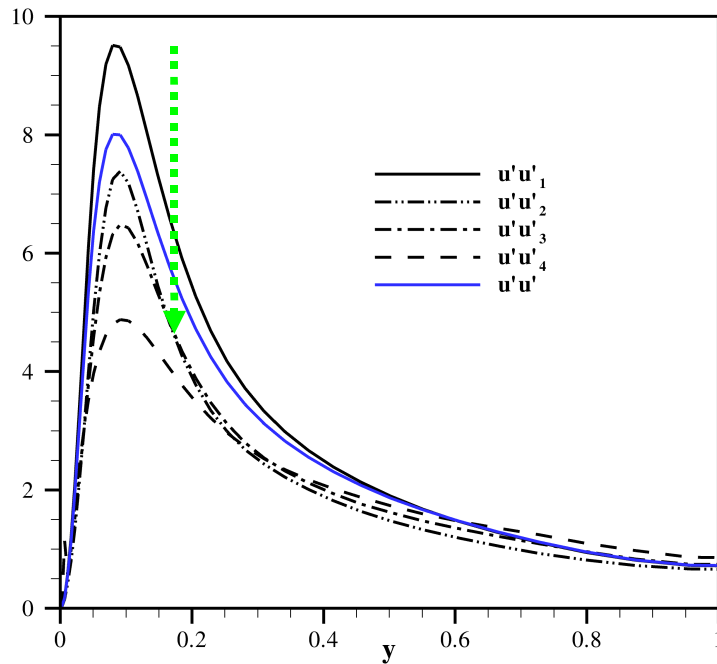
Intense vortices (or vortex cores) move slower at the channel center, and faster close to the wall



Channel flow

Streamwise velocity fluctuation

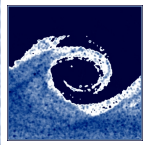
Wall-normal velocity



Q strength inversely prop.
to streamwise fluctuation

Vortex core tends to the center
perimeter to the wall



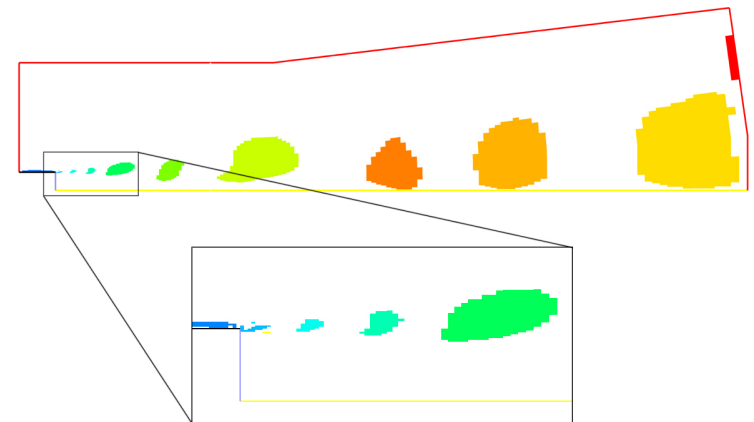
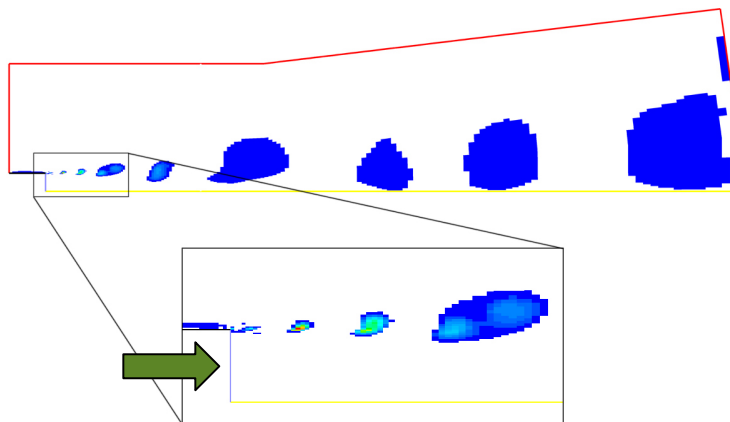


Vortex tracking

- Vortices need to be identified separately
 - The educted region needs to be divided into disjunct sets
- Needed for the quantitative investigation of the interactions

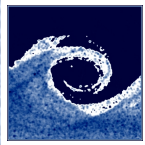
The complete educted region

Vortices with indices



Example of an axisymmetric jet

(Nyers2008)

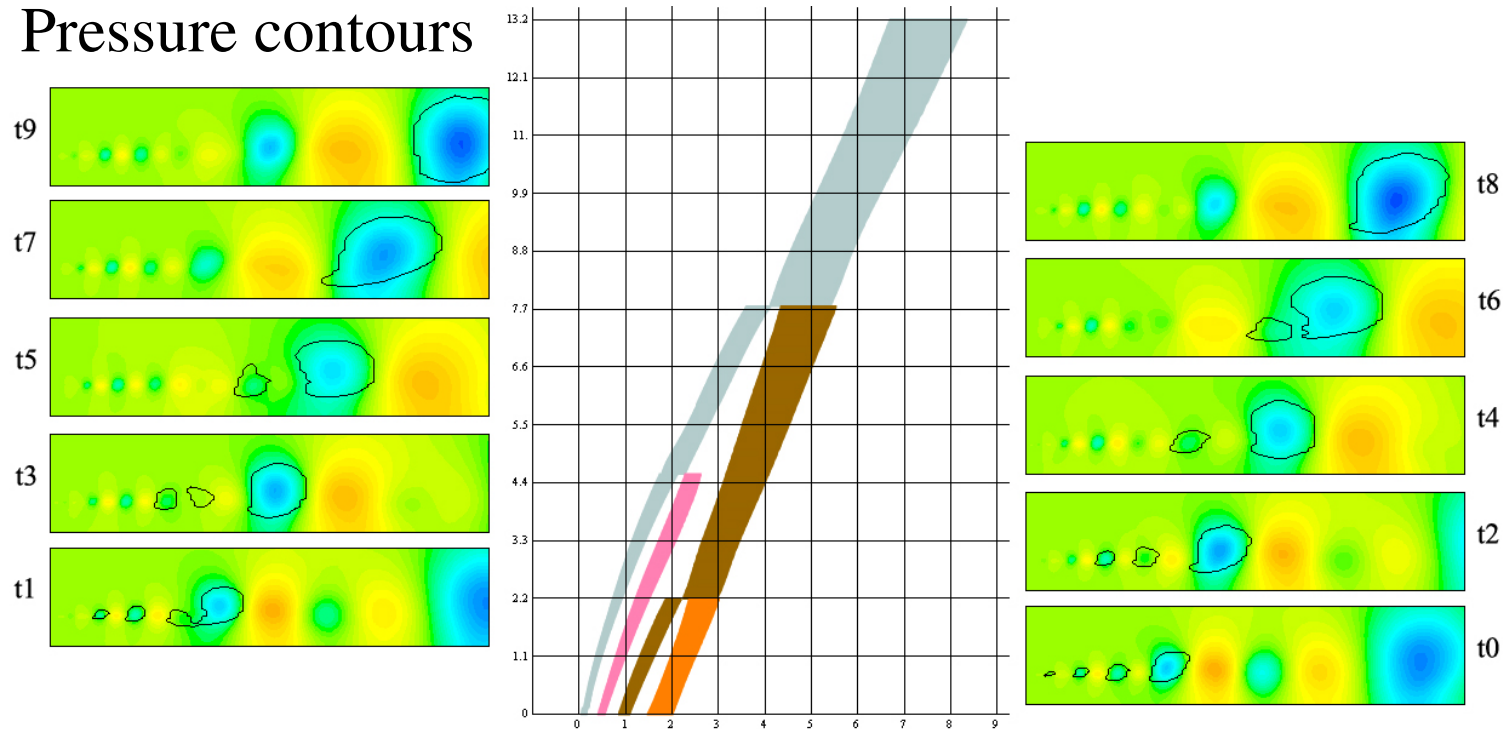


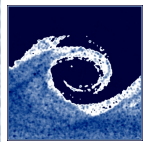
Vortex tracking

Application example:

Position and size of the vortices

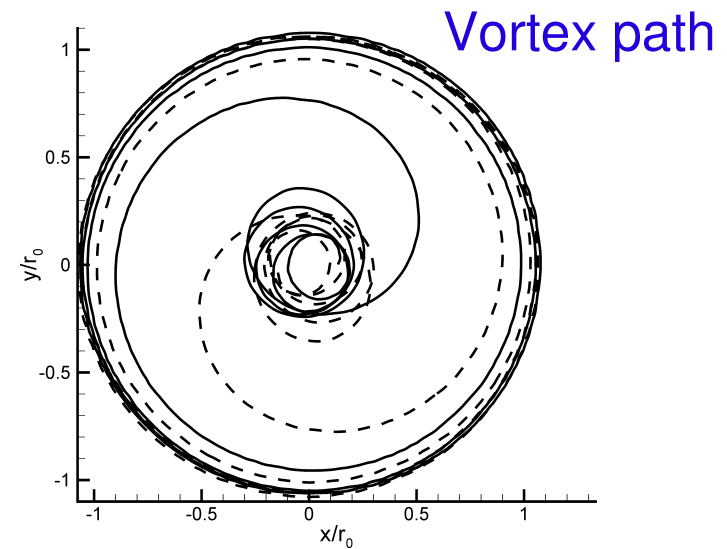
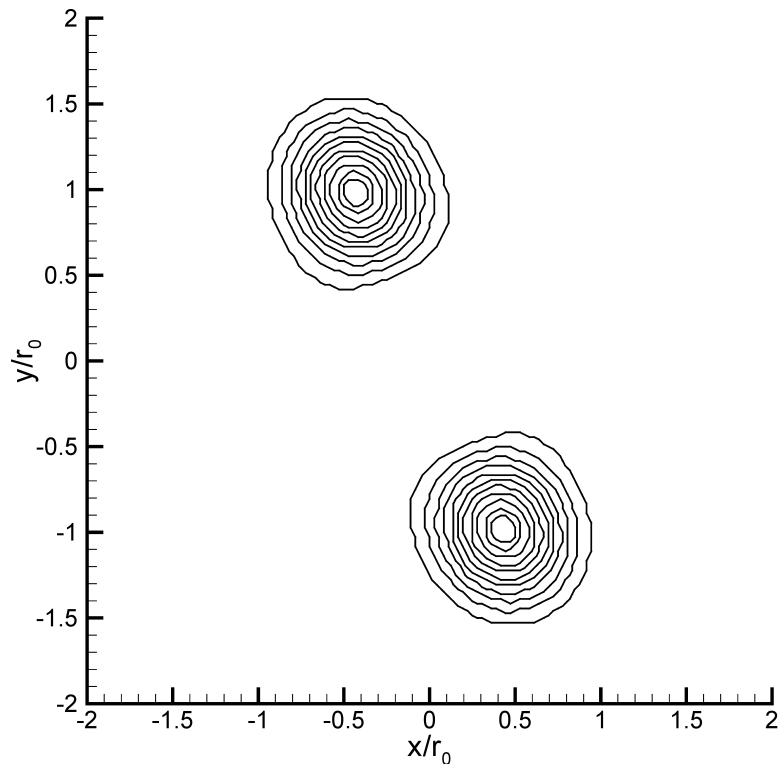
Pressure contours



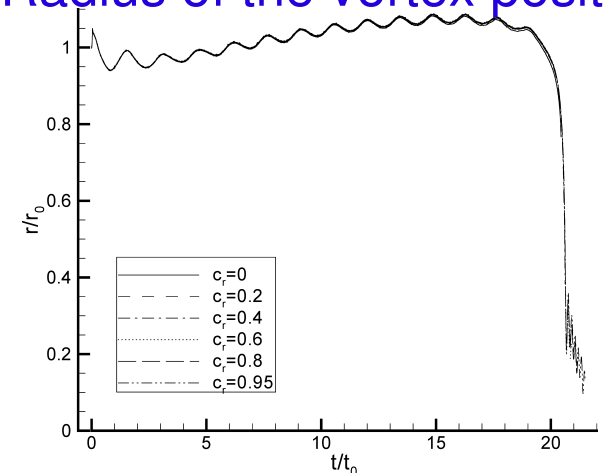


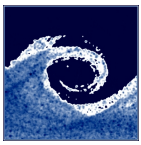
Spinning, merging vortices

Spinning vortex pair,
different threshold



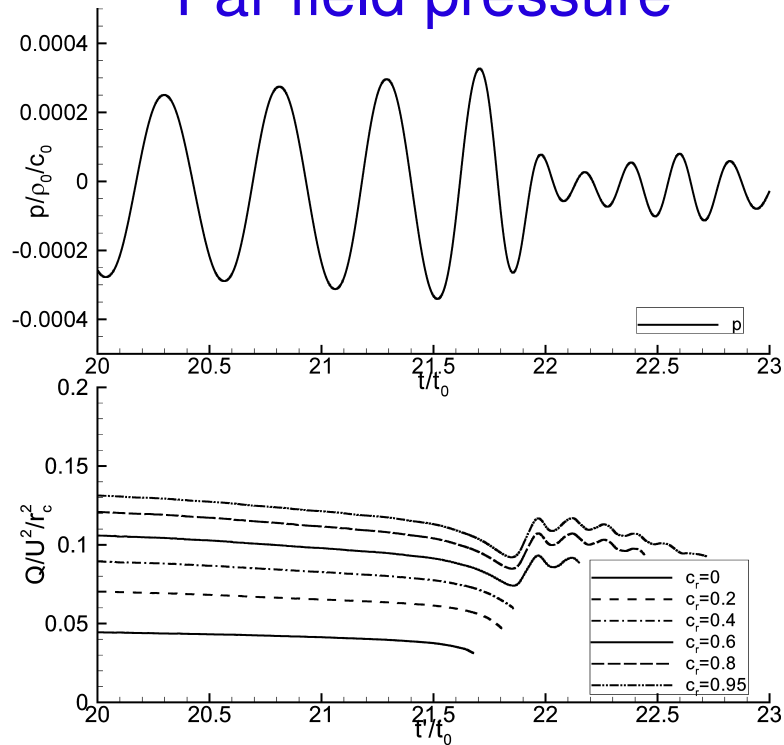
Radius of the vortex position



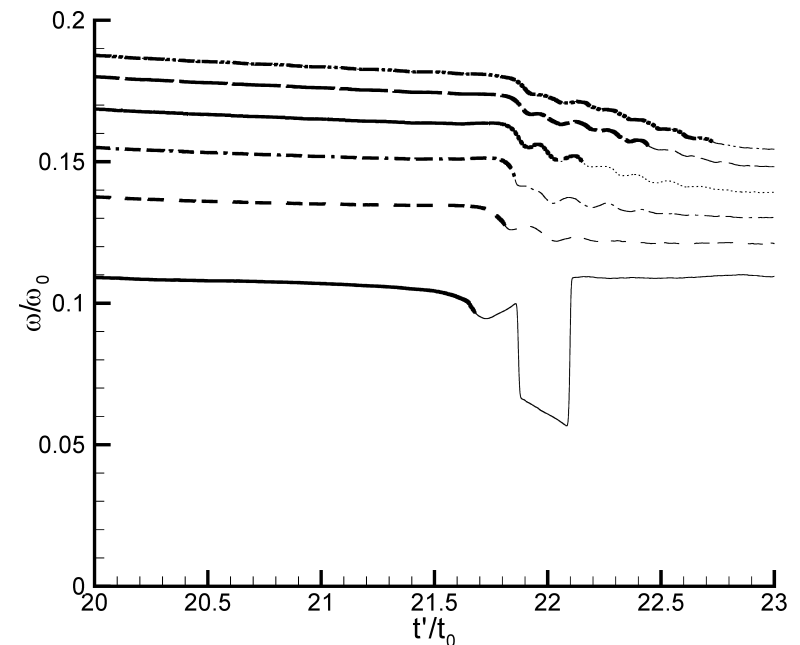


Correlation between noise and vortices

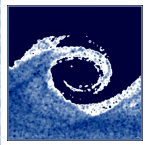
Far field pressure



Average vorticity evolution



Goal: Prediction of far field sound using vortex position and strength evolution



Conclusion

The combination of the two methods:

A tracking based averaging could provide the best understanding of the vortex evolution

Thank you for your attention!